

# 國立清華大學數學系訪問學者學術演講

## NTHU Department of Mathematics

### Visiting Scholar Colloquium

講題 Decomposing tensor product by Dirac cohomology

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時間 2024.8.27 (Tue.) 14:00 – 15:00

地點 綜合三館4F Lecture Room B

#### Abstract

Let  $g$  be a complex semisimple Lie algebra. Let  $F$  be a finite-dimensional  $g$ -module with weights  $\mu_1, \dots, \mu_k$ , and  $X$  be an arbitrary  $g$ -module with infinitesimal character  $\chi_\lambda$ . Kostant proved that an infinitesimal character which occurs in the tensor product of  $X \otimes F$  is necessarily of the form  $\chi_{\lambda+\mu_i}$  ( $i = 1, \dots, k$ ). However, it is a difficult question whether a nonzero submodule with infinitesimal character  $\chi_{\lambda+\mu_i}$  indeed occurs in  $X \otimes F$ . Assume  $X$  is a Harish-Chandra module with infinitesimal character  $\chi_\lambda$ . We prove a criterion when a nonzero submodule with infinitesimal character  $\chi_{\lambda+\mu_i}$  occurs in  $X \otimes F$  by using Dirac cohomology.