

1. T/F 正確 (2)

14 知道要證明 $\lim_{x \rightarrow 0} \frac{f(x) - (x+2)}{x} = 0$ (2~3)

寫出 $\left| \frac{f(x) - (x+2)}{x} \right| \leq |x|^{0.1} |\ln|x|| \quad (x \neq 0)$ (4)

解釋 $\lim_{x \rightarrow 0} |x|^{0.1} |\ln|x|| = 0$ (2)

$$\lim_{x \rightarrow 0} \frac{f(x) - 2}{x - 0} = \lim_{x \rightarrow 0} \frac{f(x) - x - 2}{x} \quad (-3)$$

2-6 f diff. at $x=0$ (2) Explain $\lim_{x \rightarrow 0} x^2 \sin(\frac{1}{x}) = 0$ (2)

8 f' not diff. at $x=0$ (2) Formula of $f'(x)$ ($x \neq 0$) (2~3)

Explain $\lim_{x \rightarrow 0} \cos(\frac{1}{x})$ does not exist (2)

5. 寫成 $\int_a^b f(x) dx$, but with wrong $f(x)$ (6)

$$6. \quad y'(x) = \frac{1}{2} \tan^2 x + 2 \quad , \quad y(x) = \frac{3}{2} x + \frac{1}{2} \tan x + 1$$

(5) (2) (5) (2)

#4

送分 (+14)

~~$y'(x) > 0$~~ (+3)

$y(0) = -1, y'(x) > 1$ (+7)

from IVT+MVT $\Rightarrow$ exactly 1 solution

#3.

(a.) (8分) 羅必達算錯 $-2 \sim -4$

(b.) (8分) 拆成 $\frac{x}{\sin x} \cdot \frac{x}{\sin x} \cdot \frac{\cos \frac{1}{x}}{\frac{1}{x}}$ (+4)

$\frac{x}{\sin x} \rightarrow 1$ (+2) $\frac{\cos \frac{1}{x}}{\frac{1}{x}}$ (+2)

#7.

(a.) 答案 -2 沒 + C -2 u 沒換回來 -2

(b.) 替換法正確 (+2)

替換後積分整理正確 (+2)

積分正確 (+4)