## Study guide for Final Exam

Review the study guides for quiz 08 - quiz 10. They are all relevant for Final Exam.

1. Section 7.4: Study the trick on page 6 of Lecture 15 for fast comparison among logarithmic functions, polynomials and exponential functions.
2. Section 8.3: Which of the integrals $\int \sin ^{m} x \cos ^{n} x d x$ can be integrated directly? ( $m, n$ even or odd?) Which of them requires integration by parts twice to reduce $m$ or $n$ ? ( $m, n$ even or odd?) See also the table on page 484.
3. Section 8.3: Memorize the identity (2) in the table on page 484 (double angle formula) and identities (3), (4), (5) on page 487 (Products of Sines and Cosines) to be used for for small even numbers $m$ and $n$.
4. Section 8.4: Study which trigonometric substitution to be used for $a^{2}+x^{2}, a^{2}-x^{2}$ and $x^{2}-a^{2}$, respectively. Study the corresponding range of $\theta$ to determine the signs of $\sqrt{\cos ^{2} \theta}, \sqrt{\tan ^{2} \theta}, \sqrt{\sec ^{2} \theta}$, etc. when they emerge. Study how to complete a square such as $4 x^{2}-x, x^{2}+x+1$, etc.
5. Section 8.5: Study the summary on page 495 and how to find the numbers $A_{i}$ 's, $B_{j}$ 's and $C_{j}$ 's.
6. Chapter 8: Study the "half-angle substitution" $z=\tan \left(\frac{x}{2}\right)$ and problems 41-50 on page 547-548.
7. Chapter 8: If time permits, practice Chap 8, Practice Exercises problems 69-115 on page 545 as an overall review of the techniques of integration.
