

$$\frac{x^{10}-1}{x^3-1}$$

$$\frac{(x-1)(x^9+\dots+x+1)}{(x-1)(x^2+x+1)}$$

$$\lim_{x \rightarrow 0} |x| \cos\left(\frac{1}{x^2}\right) \quad -1 < \cos\left(\frac{1}{x^2}\right) < 1$$

$$= 0 \cdot \cos\left(\frac{1}{x^2}\right)$$

$$= 0$$

$$3. \quad -26$$

$$\lim_{x \rightarrow c} (3f(x) + 4g(x))$$

Given $\epsilon > 0$

$$\exists \delta_1 > 0 \text{ s.t. } 0 < |x-c| < \delta_1 \Rightarrow |f(x) - L| < \frac{\epsilon}{3}$$

$$\exists \delta_2 > 0 \text{ s.t. } 0 < |x-c| < \delta_2 \Rightarrow |g(x) - M| < \frac{\epsilon}{4}$$

$$\exists \delta_3 > 0 \text{ s.t. } 0 < |x-c| < \delta_3 \Rightarrow |h(x) - N| < \frac{\epsilon}{5}$$

$$\delta = \min\{\delta_1, \delta_2, \delta_3\}$$

$$\text{for } 0 < |x-c| < \delta \Leftrightarrow |3f(x) + 4g(x) - 5h(x) - L| < \epsilon$$

for all $\epsilon > 0$, there exists $\delta > 0$

$$0 < |x-c| < \delta \Rightarrow |f(x) - L| < \epsilon$$

$$(x-1)^2 = 4$$