Brief solutions to selected problems in homework week 05

Sec 2.6

61. For any M ?0, take
$$\delta = \left(\frac{1}{M}\right)^{\frac{1}{2}} > 0$$
 s.t.

1a) If $0 < x < \delta$ then $f(x) \ge \frac{1}{x^{\frac{1}{3}}} > \frac{1}{\delta^{\frac{1}{5}}} = M$

(b) If $0 < x < \delta$ then $f(x) \ge \frac{1}{x^{\frac{1}{3}}} > \frac{1}{\delta^{\frac{1}{5}}} = M$

(c) If $0 < x < 1 < \delta$ then $f(x) \ge \frac{1}{(x < 1)^{\frac{1}{3}}} > \frac{2}{\delta^{\frac{1}{3}}} = 2M$

M

(d) If $0 < 1 - x < \delta$ then $f(x) \ge \frac{1}{(x < 1)^{\frac{1}{3}}} > \frac{2}{\delta^{\frac{1}{3}}} = 2M$

85. $\lim_{x \to \infty} \left(|x + \frac{1}{3}x| - |x - \frac{1}{3}x| \right) = \lim_{x \to \infty} \frac{5x}{\sqrt{x^{\frac{1}{3}}x} + \sqrt{x^{\frac{1}{3}}x} + \sqrt{x^{\frac{1}{3}}x} + \sqrt{x^{\frac{1}{3}}x}}$

$$= \lim_{x \to \infty} \frac{5}{\sqrt{1 + \frac{2}{x}} + \sqrt{1 + \frac{2}{x}}}$$

($\lim_{x \to \infty} \frac{5}{x} = 2M > M$

85. $\lim_{x \to \infty} \left(|x + \frac{1}{3}x| - \sqrt{x^{\frac{1}{3}}x} + \sqrt{x^{\frac{1}{3}}x}$

Figure 1: Brief answers to selected problems in section 2.6, part 1

Figure 2: Brief answers to selected problems in section 2.6, part 2

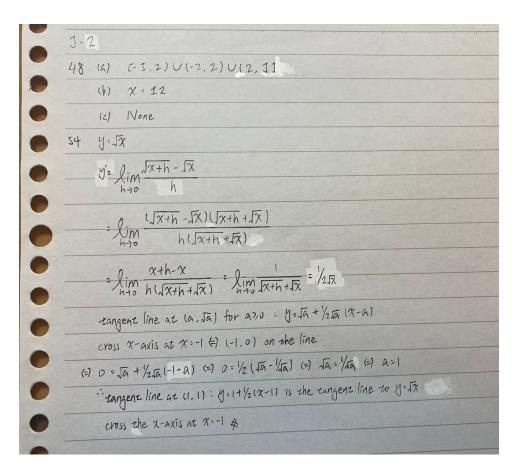


Figure 3: Brief answers to selected problems in section 3.2

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4. of x | fn(x) for x)

= 4/x | fn(x) for x)

= 4/x (fn(x) for x)

= fn(x) for x) + fn(x) for x)

= fn(x) for x)

= fn(x) for x) + fn(x) for x)

= fn(x) fn(x)

= fn(x) f
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Figure 4: Brief answers to selected problems in section 3.3