Brief answer to selected problems in HW02

- 1. No. For example. $\lim_{x\to 1} f(x) = 1$. Yet, for any $\delta > 0$, one can take $\epsilon_0 = \delta/4$ and $x_0 = 1 + \delta/4$ satisfying the definition.
- 2. Section 2.4: Problem 26 (answer = 2), 34 (answer = 1), 42 (answer = 1).
- 3. Section 2.5:

Problem 64: If f is discontinuous at g(0), f(g(x)) may still be discontinuous at x = 0. No contradiction.

Problem 67: The function g(x) = f(x) - x satisfies $g(0) \cdot g(1) \leq 0$. If the equality holds, then c is found. Otherwise, apply the Intermediate Value Theorem to g(x) on [0,1].

Problem 77: The function $f(x) = \cos(x) - x$ satisfies $f(0) \cdot f(1) < 0$.

4. Section 2.6:

Problem 92: If B > 0, take $\delta = 1/\sqrt{B}$ will do. If $B \le 0$, take δ to be any positive real number (for example $\delta = 1$) will do.

Problem 93:

- (a): change $x_0 < x < x_0 + \delta$ to $x_0 \delta < x < x_0$.
- (b): change f(x) > B to f(x) < B (or f(x) < -B).
- (c): apply both changes in (a) and (b).