

## Brief answer to selected problems in Homework 07

### 1. Section 4.2:

problem 17(b): The new polynomial is the derivative of the original polynomial. Apply Rolle's Theorem to the original polynomial.

problem 18: Apply Rolle's Theorem to  $f$ , then to  $f'$ .

problem 65: Apply mean value theorem to  $f$  on  $[0, x]$ .

problem 66: Apply mean value theorem to  $\sin(x)$  on  $[a, b]$ .

### 2. Section 4.3:

problem 74: Solve for  $a, b, c, d$  from  $f(0) = 0$ ,  $f(1) = -1$ ,  $f'(0) = 0$  and  $f'(1) = 0$ .

problem 80: (a): Show that  $f(x) = e^x - (1+x)$  satisfies  $f(0) = 0$  and  $f$  is increasing on  $x \geq 0$ . (b): Show that  $g(x) = e^x - (1+x+x^2/2)$  satisfies  $g(0) = 0$  and  $g$  is increasing on  $x \geq 0$  using the result in (a).