Calculus II, Fall 2014 (http://www.math.nthu.edu.tw/~wangwc/)

Homework Assignment for Week 15

1. Section 16.3: Problems 1, 3, 5, 9, 11, 19, 21, 26, 29, 33.

2. Let
$$F = \frac{x}{\sqrt{x^2+y^2}} i + \frac{y}{\sqrt{x^2+y^2}} j + 0k$$
 and $G = \frac{-y}{x^2+y^2} i + \frac{x}{x^2+y^2} j + 0k$.

- (a) Show that both F and G satisfy the component test.
- (b) The natural domain for both F and G is $\{(x, y, z), x^2 + y^2 \neq 0\}$ (that is where F and G are defined). Show that F is conservative in this domain by finding its potential function.
- (c) Show that G is NOT conservative in this domain (read example 5).
- (d) If given another \boldsymbol{H} satisfying the component test in this domain, how do you determine whether \boldsymbol{H} is conservative?
- 3. Let $\mathbf{F} = \frac{x}{\sqrt{x^2+y^2+z^2}} \mathbf{i} + \frac{y}{\sqrt{x^2+y^2+z^2}} \mathbf{j} + \frac{z}{\sqrt{x^2+y^2+z^2}} \mathbf{k}$. What is the natural domain for \mathbf{F} ? Show that \mathbf{F} satisfies the component test in this domain. Is this domain simply connected? Is \mathbf{F} conservative in this domain?