

Preparation guide for Quiz 04

1. Implementation of elementary numerical quadratures such as composite trapezoidal rule, composite midpoint rule and composite Simpson's method.
2. Study the error bound of above mentioned elementary numerical quadratures, both in terms of the Intermediate Value Theorem and in terms of the integral of higher order derivatives as shown in exercise set 4.4.
3. Study the definition of degree of precision, and how to derive the (closed and open) Newton-Cotes formula from degree of precision.
4. Study the relation between degree of precision and the error formula. (That is, if the degree of precision is n , what would be the general form of the error of the numerical quadrature?)
5. Study Gaussian quadrature on how to obtain the quadrature points and the weights. Both from the degree of precision approach and the roots of Legendre polynomials' approach.
6. Study how to treat the singular parts of improper integrals. Both on the unbounded integrand case and the infinite domain case.