

1. Algorithm 4.4 with $n = m = 4$ gives:
 - (a) 0.3115733
 - (b) 0.2552526
 - (c) 16.50864
 - (d) 1.476684
2. Algorithm 4.4 gives:
 - (a) 0.3115733 with $n = m = 2$
 - (b) 0.2552526 with $n = m = 4$
 - (c) 16.50864 with $n = m = 4$
 - (d) No result since it requires $n, m > 800$.
3. Algorithm 4.4 with $n = 4$ and $m = 8$, $n = 8$ and $m = 4$, and $n = m = 6$ gives:
 - (a) 0.5119875, 0.5118533, 0.5118722
 - (b) 1.718857, 1.718220, 1.718385
 - (c) 1.001953, 1.000122, 1.000386
 - (d) 0.7838542, 0.7833659, 0.7834362
 - (e) -1.985611 , -1.999182 , -1.997353
 - (f) 2.004596, 2.000879, 2.000980
 - (g) 0.3084277, 0.3084562, 0.3084323
 - (h) -22.61612 , -19.85408 , -20.14117
4. Algorithm 4.4 gives:
 - (a) 0.51184555 with $n = m = 14$
 - (b) 1.7182827 with $n = m = 20$
 - (c) 1.00000081 with $n = m = 28$
 - (d) 0.78333417 with $n = m = 20$
 - (e) -1.99999913 with $n = m = 44$
 - (f) 2.00000092 with $n = m = 34$
 - (g) 0.30842563 with $n = m = 12$
 - (h) -19.73920977 with $n = m = 144$
5. Algorithm 4.5 with $n = m = 2$ gives:
 - (a) 0.3115733
 - (b) 0.2552446
 - (c) 16.50863
 - (d) 1.488875

6. Algorithm 4.5 gives:

- (a) 0.3115733 with $n = m = 2$ and 4 function evaluations
- (b) 0.2552519 with $n = m = 3$ and 9 function evaluations
- (c) 16.508640 with $n = m = 3$ and 9 function evaluations
- (d) no result, since it requires $n, m > 5$

7. Algorithm 4.5 with $n = m = 3$, $n = 3$ and $m = 4$, $n = 4$ and $m = 3$, and $n = m = 4$ gives:

- (a) 0.5118655, 0.5118445, 0.5118655, 0.5118445, 2.1×10^{-5} , 1.3×10^{-7} , 2.1×10^{-5} , 1.3×10^{-7}
- (b) 1.718163, 1.718302, 1.718139, 1.718277, 1.2×10^{-4} , 2.0×10^{-5} , 1.4×10^{-4} , 4.8×10^{-6}
- (c) 1.000000, 1.000000, 1.000000, 1.000000, 0, 0, 0, 0
- (d) 0.7833333, 0.7833333, 0.7833333, 0.7833333, 0, 0, 0, 0
- (e) -1.991878 , -2.000124 , -1.991878 , -2.000124 , 8.1×10^{-3} , 1.2×10^{-4} , 8.1×10^{-3} , 1.2×10^{-4}
- (f) 2.001494, 2.000080, 2.001388, 1.999984, 1.5×10^{-3} , 8×10^{-5} , 1.4×10^{-3} , 1.6×10^{-5}
- (g) 0.3084151, 0.3084145, 0.3084246, 0.3084245, 10^{-5} , 5.5×10^{-7} , 1.1×10^{-5} , 6.4×10^{-7}
- (h) -12.74790 , -21.21539 , -11.83624 , -20.30373 , 7.0, 1.5, 7.9, 0.564

8. Algorithm 4.5 with $n = m = 5$ gives:

- (a) 0.51184464, error 3×10^{-10}
- (b) 1.7182816, error 2.2×10^{-7}
- (c) 1.0000000, error 0
- (d) 0.78333333, error 0
- (e) -1.9999989 , error 1.1×10^{-6}
- (f) 2.0000001, error 1.1×10^{-7}
- (g) 0.30842509, error 4.3×10^{-8}
- (h) -19.712428 , error 0.0268

9. Algorithm 4.4 with $n = m = 14$ gives 0.1479103, and Algorithm 4.5 with $n = m = 4$ gives 0.1506823.

10. $\iint_R \sqrt{xy + y^2} \, dA \approx 13.15229$

11. The approximation to the center of mass is $(\bar{x}, \bar{y})$, where $\bar{x} = 0.3806333$ and $\bar{y} = 0.3822558$.

12. The approximation from Algorithm 4.5 with $n = m = 5$ is $\bar{x} = 0.3820547$ and $\bar{y} = 0.3813976$.

13. The area is approximately 1.0402528.

14. The area approximation from Algorithm 4.5 is 1.0402523.

15. Algorithm 4.6 with $n = m = p = 2$ gives the first listed value. The second is the exact result.
- (a) 5.204036, $e(e^{0.5} - 1)(e - 1)^2$
 - (b) 0.08429784, $\frac{1}{12}$
 - (c) 0.08641975, $\frac{1}{14}$
 - (d) 0.09722222, $\frac{1}{12}$
 - (e) 7.103932, $2 + \frac{1}{2}\pi^2$
 - (f) 1.428074, $\frac{1}{2}(e^2 + 1) - e$
16. Gaussian quadrature with $n = m = p = 3$ gives:
- (a) 5.206442
 - (b) 0.08333333
 - (c) 0.07166667
 - (d) 0.08333333
 - (e) 6.928161
 - (f) 1.474577
17. Algorithm 4.6 with $n = m = p = 4$ gives the first listed value. The second is from Algorithm 4.6 with $n = m = p = 5$.
- (a) 5.206447, 5.206447
 - (b) 0.08333333, 0.08333333
 - (c) 0.07142857, 0.07142857
 - (d) 0.08333333, 0.08333333
 - (e) 6.934912, 6.934801
 - (f) 1.476207, 1.476246
18. Gaussian quadrature with $n = m = p = 4$ gives 3.0521250. The exact result is 3.0521249.
19. The approximation 20.41887 requires 125 functional evaluations.